

Utilisation des propriétés

Source *Sésamath*

Exercice corrigé pas à pas



- 1 Calculer $\sin \frac{5\pi}{4}$, $\sin \left(-\frac{\pi}{4}\right)$ et $\sin \frac{5\pi}{6}$.
- 2 On sait que $\cos \left(\frac{2\pi}{5}\right) = \frac{\sqrt{5} - 1}{4}$.
En déduire $\sin \left(\frac{\pi}{10}\right)$.

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